# B I T C O I N 

## A PEER-TO-PEER ELECTRONIC <br> C A S H S Y S T E M

Abstract. A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending.

We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone


#### Abstract

1. Introduction inancial institutions serving as come trusted rely almost exclusively on electronic payments. While the system works well enough for most transactions, it still suffers from the inherent weaknesses of the trust based model. Completely non-reversible transactions are not really possible, since financiail institutions cannot avoid mediating disputes. The eost of mediation the minimum practical transaction size and cutting off the possibility for small casual transactions, and there is a broader cost in the loss of ability to make non-reversible payments for nonreversible services. With the possibility of reversal, the need for nonreversible services. With the possibility of reversal, the need for trust spreads. Merchants must be wary of their customers, hassling them for more information than they would otherwise need. A d percentage of fraud is accepted as unavoidable. These costs and payment uncertainties can be avoided in person by using physical currency, but no mechanism exists to make payments over communications channel without a trusted party. What is needed is an electronic payment system based on cryptographic proof with each other without the need for a trusted third party. protect sellers from fraud, and routine escrow mechanisms could easily be implemented to protect buyers. In this paper, we propose a solution to the double-spending problem using a peer-to-peer the chronological order of transactions. The system is secure as long as honest nodes collectively control more CPU power than any nodes. 2. Transactions derine an electronic coin as a chain of digital signatures. Each a previous transaction and the public key of the enext owner and adding these to the end of the coin. A payee can verify the


 The problem of course is the payee can't verify that one of the
owners did not double-spend the coin. A common solution is to introduce a trusted central authority, or mint, that checks every
transaction for double spending. After each transaction, the coin must be returned to the mint to issue a new coin, and only coins ssued directly from the mint are trusted not to be double-spent.
The problem with this solution is that the fate of the entire money he problem with this solution is that the fate of the entire money
system depends on the company running the mint, with every ransaction having to go through them, just like a bank. We need a ay forl the payee to know that the previous owners did not sign the one that counts, so we don't care about later attempts to to be aware of all transaytions in the the absence of a transaction was aware of all transactions and decided which arrived first. To
accomplish this without a trusted publicly announced [1], and we need a system for participants to agree on a single history of the order in which they were received.
The payee needs proof that at the time of each transaction, the 3. Timestamp
mestamp server works by taking a hash of a block of items to be mestamped and widely publishing the hash, such as in a
ewspaper or Usenet post [ $2-5$ ]. The timestamp proves that the data must have existed at the time, obviously, in order to get into he hash. Each timestamp includes the previous timestamp in its
ash, forming a chain, with each additional timestamp reinforcing hash, forming a chain, with each additional timestamp reinforcing
the ones before it

| - Hash |  | $\rightarrow$ Hash |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Block |  | Block |  |  |
| Hem | Item | Item | Hem | ... |

4. Proof-of-Work
basis, we will need to use a prootof-work syst on a peer-to-peer Back's Hashcash [6], rather than newspaper or ssenet po Adam oof-of-work involves scanning for a value that when hashed, such as with SHA-256, the hash begins with a number of zero bits. The equired and can be verified by executing number of zero bits mestamp network, we implement the proof-of-work by crementing a nonce in the block until a value is found that gives the block's hash the required zero bits. Once the CPU effort has been expended to make it satisfy the proof-of-work, the block
cannot be changed without reding the work. As later blocks are lock would include

nodes until he's convinced he has the longest chain, and obtain the
Merkle branch linking the transaction to in. He can't check the transaction for himself, but by linking it to a place in the chain, he can see that a n nework node has accepted it,
and blocks added after it further confirm the network has accepted

5. Combining and Splitting Value

Although it would be possible to handle coins individually, it would transfer. To allow value to be split and combined, transaction single input from a larger previous transaction or multiple inputs
combining smaller amounts, and at most two outputs: one for the payment, and one returning the change, if any, back to the sender.

It should be noted that fan-out, where a transaction depends on several transactions, and those transactions depend on many more,
is not a problem here. There is never the need to extract a complete 10. Privacy
access to information to the parties involved and the trusted third party. The necessity to announce all transactions publicly precludes this method, but privacy can still be maintained by breaking the
flow of infor nonymous. The public can see that someone is sending public keys to someone else, but without information linking the transaction to anyone. This is similar to ter exchanges, where the time and size of individual trades, the "tape"
is made public,

$\qquad$ As an additional firewall, a new key pair should be used for each
transaction to keep them from being linked to a common owner Some linking is still unavoidable with multi-input transactions,
which necessarily reveal that their inputs were owned by the same owner. The risk is that if the owner of a key is revealed, linking

## 11. Calculations

We consider the scenario of an attacker trying to generate an accomplished it changes, such as creating value out of thin air or taking money that never belonged to the attacker. Nodes are not going to accept an
invalid transaction as payment, and honest nodes will never accep a block containing them. An attacker can only try to change one of his own transactions to take back money he recently spent. Th
race between the honest chain and an attacker chain can b characterized as a Binomial Random Walk. The success event is the honest chain being extended by one block, increasing its lead by +1 , and the failure event is the attacker's chain being extended by one
block, reducing the gap by -1 . The probability of an attacker catching up from a given deficitit is analogous to a Gambler's Ruin
ner problem. Suppose a gambler with unlimited credit starts at a deficit and plays potentially an infinite number of trials to try to reach breakeven. We can calculate the probability he ever reaches
breakeven, or that an attacker ever catches up with the honest chain, as folliows 8 :
$p=$ probability an honest node finds the next block
$q=$ probability the attacker finds the next block
$q_{2}=$ probability the attacker will ever catch $q_{z}=\left\{\begin{array}{cc}1 & \text { if } p \leq q \\ (q / p)^{2} & \text { if } p>q\end{array}\right\}$
Given our assumption that $p>q$, the probability drop exponentially as the number of blocks the attacker has to catch up lucky lunge forward early on, his chances become vanishingly smal as he falls further behind. We now consider how long the recipien
the sender can't change the transaction. We assume the sender is antacker who wants to make the recipient believe he paid him for a while, then switch it to pay back to himself after some time as passed. The receiver will be alerted when that happens, but the
sender hopes it will be too late. The receiver generates a new he pair and gives the public key to the sender shortly before signing This prevents the sender from preparing a chain of blocks ahead of time by working on it continuously until he is lucky enough to ge far enough ahead, then executing the transaction at that moment. Once the transaction is sent, the dishonest sender starts working in
secret on a parallel chain containing an alternate version of his transaction. The recipient waits until the transaction has beeen
added to a block and $z$ blocks have been linked after it. He doesn't now the exact amount of progress the attacker has made, bu assuming the honest blocks took the average expected time per with expected value:
$\lambda=\frac{z q}{p}$
o get the probability the attacker could still catch up now, we multiply the Poisson density for each amount of progress he could $\sum_{k=0}^{\infty} \frac{\lambda^{k} e^{-\lambda}}{k!} \cdot\left\{\begin{array}{cc}(q / p)^{(z-k)} & \text { if } k \leq z \\ \text { if } k>z\end{array}\right\}$
$\sum_{==1}^{z} \frac{\lambda^{k} e^{-\lambda}}{k!}\left(1-(q / p)^{\left(z^{-k}\right)}\right)$
Converting to C cod
include $<$ math.h
>

```
ouble Attackersu
```


## double $p=1.0-q$ double lambda $=\Sigma$

double sum =1.0;

for ( $\mathrm{i}=$ esson
or $(i)=1 ; i<k ; i++)$
poisson $*=$ lambda
sum $-=\operatorname{poisson}^{*}(1-\operatorname{pow}(q / \mathrm{p}, \mathrm{z}-\mathrm{k})$.




 $P=0.0000379 \quad$
$P=0.0000006$ Solving for $P$ less than 0.1\%... $P<0.001 \quad q=0.10 \quad z=5 q=0.15 \quad z=8$
$q=0.20 \quad z=11 \quad$ = $=0.25 \quad z=15 \quad q=0.30 \quad z=24 \quad=0.35 \quad z=41$ 12. Conclusion
elying on trust. We started with the usual framework of coins made from digitial sigartures, which provides strong control of
meth ownership, but is incomplete without a way to prevent double-
spending. To solve this, we proposed a peer-to-peer network using proof-of-work to record a public history of transactions that quickly becomes computationally impractical for an attacker to change if honest nodes control a majority of CPU power. The network is robust in its unstructured simplicity. Nodes work all at once with
little coordination. They do not need to be identified, since messages are not routed to any particular place and only need to be
delivered on a best effort basis. Nodes can leave and rejoin the network at will, accepting the proof-of-work chain as proof of what
happened while they were gone. They vote with their CPU power, happened while they were gone. They vote with their CPU power,
expressing their acceptance of valid blocks by working on extending them and rejecting invalid blocks by refusing to work on them. Any
needed rules and incentives can be enforced with this consensus

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